Supplementary Material

Dose-Responses from Multi-Model Inference for the Non-cancer Disease Mortality of Atomic Bomb Survivors

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1. Preston baseline model

The Preston baseline model is as follows:

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h_0 = \exp\{cmH + cfH + cmN + cfN + e30170 \times e30 \times lage70 + e30m \times e30 + e30f \times e30
+ e30sqm \times e30sq + e30sqf \times e30sq + e30qspm \times e30qsp + e30qspf \times e30qsp
+ e50qspm \times e50qsp + e50qspf \times e50qsp + 170m \times lage70 + 170f \times lage70
+ 170sqm \times lage70sq + 170sqf \times lage70sq + 140qspm \times lage40qsp + 140qspf \times lage40qsp +
+ 170qspm \times lage70qsp + 170qspf \times lage70qsp\}
(A1)
with e30 := (e - 30)/10, e30sq := e30 × e30, e50 := (e - 50)/10,
lage70 := ln(a/70), lage70sq := ln(a/70) \times ln(a/70),
e30qsp := [e30] \times [e30] for e > 30,
e50qsp := [e50] \times [e50] for e > 50,
lage40qsp := [ln(a/40)] \times [ln(a/40)] for a \ge 40,
lage70qsp := [ln(a/70)] \times [ln(a/70)] for a \ge 70.
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These naming conventions are taken from R13models.log. Age at exposure is denoted by *e*, age attained by *a*. Model parameters in Eq. (A1) are italicised. Parameters *cmH*, *cfH*, *cmN*, and *cfN* represent constant factors (*cmH* and *cfH*, for example, are constants related to males and females in Hiroshima), parameter *e30l70* describes variations of the hazard with multiplicative effects of age attained and age at exposure, while parameters *e30m* and *e30f* describe variations of the hazard with age at exposure for males and females, respectively. Parameters *e30qspm* and *e30qspf* mark

the dependence on a quadratic spline function with age knot at e = 30 years for males and females, respectively. The Preston baseline model therefore uses 29 model parameters including the four age knots in e30qsp, e50qsp, lage40qsp, and lage70qsp.

2. Streamlined baseline models

One common (i.e. joint) baseline model was used for the cerebrovascular disease (CVD) data. Our streamlined baseline model for CVD contains 21 statistically significant baseline parameters - 8 parameters less than Preston's baseline model h_0 from Eq. (A1): e30sqm = e30qspm = e50qspm = e50qspm = e50qspm = e50qspf = 170f = 0 which made the three age knots related to e30qspm, e50qspm, and e50qspm obsolete. In other words: for the fit of the CVD data one single joint baseline model was used, namely Eq. (A1) with e30sqm = e30qspm = e50qspm = e50qspm = 170f = 0. In addition, it was found that the model fit significantly improved when the age knots at 40 and 70 years in lage40qsp and lage70qsp, respectively, were allowed to be free. Note that for reasons of clarity the related adjustable parameters are denoted by 140agem, 140agef, 170agem, and 170agef although best estimates different than 40 or 70 were found in the related model fits (Table S1). The fit also significantly improved when the age at exposure knot at 30 years in e30qsp was allowed to be free; the related model parameter is denoted by e30agef.

For cardiovascular diseases, we proceeded analogously as for CVD. Each of the 29 parameters of the Preston baseline model was tested for its significance resulting in a streamlined baseline model with 14 model parameters less than the Preston baseline model: e30qspm = e30qspf = e50qspm = e50qspf = 170m = 170sqf = 170qspm = 0 with the five age knots related to e30qspm, e30qspf, e50qspm, e50qspf, and 170qspm obsolete. In other words: for the fit of the data for cardiovascular diseases one single joint baseline model was used, namely Eq. (A1) with e30qspm = e30qspf = e50qspm = e50qspf = 170m = 170sqf = 170qspm = 0. Furthermore, it was found that for cardiovascular diseases there was no statistically significant city effect: instead of the four baseline parameters cmH, cfH, cmN, and cfN applied for CVD (Table S1) only two remain for cardiovascular diseases: cm and cf (Table S2). The streamlined baseline model for cardiovascular diseases therefore has 15 (29 – 12 – 2) model parameters (see

Table S2 in the Online Resource). In addition, it was found that the model fit significantly improved when the age knots at 40 and 70 in lage40qsp and lage70qsp, respectively, were allowed to be free (Table S2).

3. Dose-effect modifiers

Three dose-effect modifiers were implemented into the various risk models. For an excess relative risk (ERR) model, the following form was applied: $h = h_0 \times (1 + ERR(D, s, a, e))$ where D, s, a, e stand for dose, sex, attained age and age at exposure, respectively. It is $ERR(D, s, a, e) = err(D) \times \exp(dem_1 \times \sec + dem_2 \times e30 + dem_3 \times lage70)$. Here, err(D) is any of the dose-responses depicted in Fig. 1. The general form of an excess absolute risk (EAR) model is $h = h_0 + EAR(D, s, a, e)$ where $EAR(D, s, a, e) = ear(D) \times \exp(dem_1 \times \sec + dem_2 \times e30 + dem_3 \times lage70)$ and ear(D) is any of the dose-responses from Fig. 1. Here, dem_1 , dem_2 , and dem_3 are three adjustable parameters related to the three dose-effect modifiers sex, age at exposure, and age attained. The naming conventions for e30 and lage70 are provided after Eq. (A1).

When fitting the mortality data for cardiovascular diseases we found for the EAR-LNT model and the EAR-quadratic model that age was a statistically significant dose effect modifier with the related parameter dem3 = 5.1 (Table S2). That gives the factor $\exp(5.1 \times \ln(a/70))$). At an attained age of a = 56 years, the mean age attained of all individuals registered within the data set for cardiovascular diseases, we therefore have $h = h_0 + 0.29 \times ear(D)$. For a = 70 years we simply have $h = h_0 + ear(D)$. Consequently, for lower ages the *EAR* (shown in Fig. 3 for a = 70 years) calculated with the EAR-LNT model is strongly decreased. This explains the seemingly inconsistent shape of the *EAR* for the EAR-LNT model in Fig. 3. Because of the relatively large weight of the EAR-LNT model (0.3619; see Table 1), the *EAR* for the MMI is then also shifted towards lower values.

For all other model fits no significant effect modifiers were found (Tables S1 and S2).

4. Poisson regression

The MECAN software (Kaiser 2010) uses the maximum likelihood method to estimate the values of the adjustable model parameters by fitting the model to the data. Because maximizing the likelihood is equivalent to minimizing the $-\ln(\text{Likelihood})$, the latter problem, which is numerically better tractable, is solved in MECAN to find the best model solution. For grouped person-year data such as the grouped LSS data, the likelihood corresponding to a Poisson model is used: $-\ln(L) = \sum_{i} \left[\Lambda_i - n_i + n_i \ln(n_i / \Lambda_i) \right]$ where n_i is the observed number of cases (i.e. the number of fatal

CVDs or cardiovascular diseases) in group i and Λ_i is the calculated (expected) number of cases in group i. The deviance is defined as $dev := -2 \times \ln(\text{MaxLikelihood})$.

5. ERR and EAR calculated from different models

For CVD, we found that two different ERR models are preferable (Table 1). The general form of an ERR model is $h = h_0 \times RR = h_0 \times (1 + ERR)$, where RR is the relative risk. Consequently, when we calculate the EAR from an ERR model we get $EAR = h - h_0 = h_0 \times (1 + ERR) - h_0 = h_0 \times ERR$. For CVD, the baseline model, h_0 , depends on city and sex via model parameters cmH, cfH, cmN, and cfN (Table S1). Therefore, the EAR-values for CVD (Table 2) also depend on city and sex: they are only valid for males from Hiroshima, as stated in the Results section of the main text. When the ERR is calculated from an ERR model, then only the shape of the dose-responses related to the excess risk from radiation enters the risk estimate. Fig. 2 is therefore valid for males and females from both cities.

For cardiovascular diseases, it was found that three different EAR *models* are preferable (Table 1). The general form of the EAR model is $h = h_0 + EAR$. When the *ERR* is calculated from an EAR model, one gets $ERR = h/h_0 - 1 = (h_0 + EAR)/h_0 - 1 = EAR/h_0$. For cardiovascular diseases, we found that h_0 is dependent on sex (but not city) via model parameters cm and cf (Table S2). Therefore, the *ERR*-values for cardiovascular diseases

(Table 3) also depend on sex: they are only valid for males. Related to Fig. 3 it can be said that the *EAR* calculated from an EAR model only depends on the shapes of the preferable dose-responses for the excess risk from radiation. Therefore, Fig. 3 is valid for males and females from both cities.

6. Derivation of city-averaged EAR-values to be used in Table 2

In the previous section it has been derived that for CVD the *EAR* can be calculated from an ERR model as follows: $EAR = h_0 \times ERR$. The city-averaged EAR-values for males, $\langle EAR \rangle_m$, can be calculated as follows:

$$\langle EAR \rangle_m = w_H \times EAR_H + w_N \times EAR_N = ERR \times (w_H \times h_{0,mH} + w_N \times h_{0,mN}). \tag{A2}$$

Here, $w_H = PY_H/PY_{tot}$ is the number of person years in Hiroshima divided by the total number of person years in the data set; $w_N = PY_N/PY_{tot}$ is the number of person years in Nagasaki divided by the total number of person years in the data set, and $h_{0,mH}$ is the streamlined baseline hazard for males in Hiroshima, i.e. Eq. (A1) with the numerical values for the model parameters taken from Table S1 using e30sqm = e30qspm = e50qspm = e50qspf = 170f = 0 (refer to section 2 above) and with cfH = cmN = cfN = 0. An analogous definition holds for $h_{0,mN}$. For the ERR-LNT model we therefore have

 $h_{0,mH} = \exp\{-9.57 + 0.44 \times e30 \times lage70 + 0.504 \times e30 + 2.07 \times e30 + 0.522 \times e30 \text{sq} - 0.581 \times e30 \text{qsp} - 11.32 \times lage70 - 14.3 \times lage70 \text{sq} - 5.6 \times lage70 \text{sq} + 16.33 \times lage40 \text{qsp} + 8.9 \times lage40 \text{qsp} - 120 \times lage70 \text{qsp} - 134 \times lage70 \text{qsp}\} = \exp\{-9.57\} \times \exp\{rest\}$ where rest stands for all other terms in the exponential function.

The right hand side of Eq. (A2) can be expanded as follows:

$$ERR \times (w_H \times h_{0,mH} + w_H \times h_{0,mN}) = ERR \times h_{0,mH} \times \left(w_H + w_N \frac{h_{0,mN}}{h_{0,mH}} \right).$$
 (A3)

With Eq. (A1) one finds

$$ERR \times h_{0,mH} \times \left(w_H + w_N \frac{h_{0,mN}}{h_{0,mH}} \right) = ERR \times h_{0,mH} \times \left(w_H + w_N \frac{e^{cmN}}{e^{cmH}} \right) = \frac{1}{2} \left(w_H + w_N \frac{e^{cmN}}{e^{cmH}} \right)$$

$$ERR \times h_{0,mH} \times \left(w_H + w_N e^{(cmN - cmH)} \right). \tag{A4}$$

Considering Eq. (A2) and using $EAR = h_0 \times ERR$ within Eq. (A4), one obtains

$$\langle EAR \rangle_m = EAR_{mH} \times \left(w_H + w_N e^{(cmN - cmH)} \right). \tag{A5}$$

The term EAR_{mH} stands for the EAR-values for males in Hiroshima as given in Table 2. The city-averaged EAR-values for males can be obtained by multiplication with the correction factor of $\left(w_H + w_N e^{(cmN-cmH)}\right)$. It is $w_H = PY_H/PY_{tot} = 818938.31/1200991.78 = 0.68$ and $w_N = PY_N/PY_{tot} = 382053.47/1200991.78 = 0.32$. Using the best estimates from Table S2, we find that for all three preferred models the correction factor is 1.1. Applying the AIC-weights from Table 1 therefore yields again the correction factor of 1.1, which can be applied to calculate from the EAR-values

for MMI in Table 2 the city-averaged *EAR*-values (for example: for the MMI the *EAR*-value at 1 Gy for males in Hiroshima with an age attained of 70 years, exposed at an age of 30 years, is 6.6 per 10^4 PY; therefore, the city-averaged *EAR*-value for males is $6.6 \times 1.1 = 7.3$ per 10^4 PY. This risk prediction holds for males in Hiroshima and Nagasaki).

7. Neglection of categorical and Gompertz models for MMI

It is noted that the categorical model (#11 in Fig. 1) is a non-nested model like those summarized in Table 1. It was, however, not used for MMI because of its very small contributions to the AIC-weights. The categorical model fit to the data for CVD yielded $\Delta AIC = 9.85$ (with dev = 3565.9 and Npar = 28). Using Eq. (2) with n = 2 and m = 1 (i.e. comparing with the best model, which has $\Delta AIC = 0$) one obtains $p_1 = \exp(-\Delta AIC_1/2)/(1+\exp(-\Delta AIC_1/2)) = 0.0072$. For cardiovascular diseases we found $\Delta AIC = 10.65$ (with dev = 3694.38, Npar = 22). That gives $p_1 = 0.0048$. Both values are far below the threshold value of 0.05 that is used as a cut-off in the scientific literature (Hoeting et al. 1999, Walsh 2007). The fit of the data for cardiovascular diseases with the Gompertz function led to $p_1 = 0.035$; therefore this model was not used for MMI either.

References

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Walsh L (2007) A short review of model selection techniques for radiation epidemiology. Radiat Environ Biophys 46:205-213

Table S1 Results from fitting the final three non-nested models to the joint mortality data for CVD in males and females: Best estimates and Wald-type standard errors (in parentheses) for the model parameters of the three preferable model fits for CVD. The numbers in brackets refer to the eleven dose-responses depicted in Fig. 1 in the main text. Parameters 1 to 21 are the baseline parameters, parameters 22 and 23 are radiation related parameters, i.e. they refer to the risk models #1, #2, and #6 depicted in Fig. 1.

	Parameter ERR-LNT model [#		ERR-quadratic model [#2]	ERR-step model ^a [#6]
1	стН	-9.57 (0.23)	-9.56 (0.24)	-9.573 (0.030)
2	сfH	-5.96 (0.14)	-5.96 (0.13)	-5.937 (0.029)
3	cmN	-9.40 (0.23)	-9.38 (0.25)	-9.404 (0.050)
4	cfN	-5.96 (0.14)	-5.96 (0.13)	-5.945 (0.044)
5	e30l70 (yr ⁻¹)	0.44 (0.18)	0.44 (0.18)	0.447 (0.043)
6	e30m (yr ⁻¹)	0.504 (0.034)	0.504 (0.034)	0.505 (0.014)
7	$e30f(yr^{-1})$	2.07 (0.11)	2.06 (0.12)	2.083 (0.012)
8	e30sqf (yr ⁻²)	0.522 (0.032)	0.520 (0.033)	0.5259 (0.0060)
9	e30qspf (yr ⁻²)	-0.581 (0.025)	-0.578 (0.026)	-0.5850 (0.0022)
10	170m	-11.32 (0.80)	-11.32 (0.85)	-11.33 (0.14)
11	170sqm	-14.3 (1.2)	-14.3 (1.3)	-14.32 (0.42)
12	l70sqf	-5.6 (1.2)	-5.6 (1.2)	-5.65 (0.45)
13	l40qspm	16.33 (0.73)	16.33 (0.79)	16.314 (0.065)
14	l40qspf	8.9 (2.1)	8.9 (2.1)	9.01 (0.17)
15	l70qspm	-120 (49)	-120 (49)	-119 (16)
16	l70qspf	-134 (47)	-134 (47)	-135 (50)
17	l40agem ^b (yr)	42.57 (0.49)	42.57 (0.49)	42.537 (0.055)
18	<i>l40agef</i> (yr)	51.3 (3.8)	51.3 (3.8)	51.44 (0.14)
19	l70agem ^c (yr)	84.0 (1.2)	84.0 (1.2)	83.98 (0.36)
20	l70agef (yr)	85.5 (1.0)	85.5 (1.0)	85.5 (1.0)
21	e30agef ^d (yr)	17.88 (0.80)	17.91 (0.88)	17.866 (0.061)
22		$err = 0.124 \text{ Gy}^{-1} (0.059)$	$err = 0.063 \text{ Gy}^{-2} (0.033)$	scale = 0.218 (0.076)
23				$D_{th} = 0.620 \text{ Gy} (< 1\%)$
	deviance	3569.51	3570.14	3566.05

^a Implemented as a hyperbolic tangent function with a fixed value for the slope s: 10^5 /Gy. This parameter does not count as a model parameter because $1/s \approx 0$ compared to all other parameter values.

^b Denotes the age knot for males in lage40qsp (refer to the naming conventions after Eq. (A1)).

^c Denotes the age knot for males in lage70qsp.

^d Denotes the age at exposure knot for females in e30qsp.

Table S2 Results from fitting the final four non-nested models to the joint mortality data for cardiovascular diseases in males and females: Best estimates and Wald-type standard errors (in parentheses) for the model parameters of the four preferable model fits for cardiovascular diseases. The numbers in brackets refer to the eleven dose-responses depicted in Fig. 1 in the main text. Parameters 1 to 15 are the baseline parameters, parameters 16 and 17 are radiation related parameters, i.e. they refer to the risk models #1, #2, #5, and #6 depicted in Fig. 1.

	Parameter	EAR-LNT model [#1]	EAR-quadratic model [#2]	EAR-threshold model [#5]	EAR-step model ^b [#6]
1	cm ^a	-6.52 (0.12)	-6.52 (0.12)	-6.51 (0.11)	-6.52 (0.12)
2	cf	-8.26 (0.17)	-8.12 (0.17)	-8.07 (0.17)	-8.06 (0.17)
3	e30170 (yr ⁻¹)	0.87 (0.17)	0.87 (0.18)	0.86 (0.17)	0.86 (0.17)
4	e30m (yr ⁻¹)	0.267 (0.037)	0.265 (0.037)	0.264 (0.036)	0.263 (0.036)
5	$e30f(yr^{-1})$	0.446 (0.040)	0.435 (0.039)	0.429 (0.038)	0.429 (0.038)
6	e30sqm (yr ⁻²)	-0.057 (0.017)	-0.057 (0.017)	-0.056 (0.017)	-0.056 (0.017)
7	$e30sqf(yr^{-2})$	-0.075 (0.018)	-0.073 (0.019)	-0.070 (0.018)	-0.070 (0.018)
8	l70f	1.89 (0.38)	2.12 (0.38)	2.20 (0.37)	2.23 (0.37)
9	170sqm	-5.43 (0.75)	-5.40 (0.76)	-5.36 (0.74)	-5.36 (0.74)
10	l40qspm	7.98 (0.59)	7.87 (0.59)	7.79 (0.57)	7.76 (0.57)
11	l40qspf	3.04 (0.18)	2.90 (0.18)	2.82 (0.18)	2.80 (0.18)
12	l70qspf	-139 (49)	140 (49)	-141 (50)	-141 (50)
13	l40agem ^c (yr)	47.1 (1.3)	46.9 (1.3)	46.7 (1.3)	46.6 (1.3)
14	l40agef (yr)	28.71 (0.83)	28.70 (0.88)	28.55 (0.88)	28.54 (0.88)
15	<i>l70agef</i> ^d (yr)	86.39 (0.86)	86.44 (0.89)	86.52 (0.86)	86.52 (0.86)
16		$ear = 8.8 \cdot 10^{-4} \text{ Gy}^{-1} \text{ pyr}^{-1}$	$ear = 3.9 \cdot 10^{-4} \text{ Gy}^{-2} \text{ pyr}^{-1}$	$ear = 2.1 \cdot 10^{-3} \text{ Gy}^{-1} \text{ pyr}^{-1}$	$scale = 1.16 \cdot 10^{-3} \text{ pyr}^{-1}$
		$(2.9 \cdot 10^{-4})$	$(1.7 \cdot 10^{-4})$	(0.0013)	$(5.0 \cdot 10^{-4})$
17		$dem_3 = 5.1 (1.4)$	4.1 (1.6)	$D_{th} = 2.01 \text{ Gy } (0.26)$	$D_{th} = 2.194 \text{ Gy} (< 1\%)$
3.5	deviance	3693.73	3694.05	3695.0	3695.66

^a Parameter *cm* is a constant related to males.

^b Implemented as a hyperbolic tangent function with a fixed value for the slope s: $10^5/\text{Gy}$. This parameter does not count as a model parameter because $1/s \approx 0$ compared to all other parameter values.

^c Denotes the age knot for males in lage40qsp (refer to the naming conventions after Eq. (A1)).

^d Denotes the age knot for females in lage70qsp.

Table S3 Final deviances for CVD in males analyzed with ERR-step model: Final deviances obtained by forward calculations using the ERR-step model (with $D_{th} = 0.62$ Gy) in combination with the mortality data for CVD in males. For the calculations the best estimates from Table S1 were applied. Data were grouped into four dose categories and five age categories. As a comparison, the deviances are also shown for Preston's ERR-LNT model.

	0-20 yr	20-40 yr	40-60 yr	60-80 yr	80 yr -	sum	Preston's ERR-LNT
							model
$D \le 0.005 \text{ Gy}$	155.79					155.79	154.33
$0.005 < D \le 0.1 \text{ Gy}$	652.09				652.09	651.0	
$0.1 < D \le 0.5 \text{ Gy}$	0	9.36	106.47	256.02	150.34	522.19	530.52
D > 0.5 Gy			449.57			449.57	452.47

Table S4 Final deviances for CVD in females analyzed with ERR-step model: Final deviances obtained by forward calculations using the ERR-step model (with $D_{th} = 0.62$ Gy) in combination with the mortality data for CVD in females. For the calculations the best estimates from Table S1 were applied. Data were grouped into five dose categories and five age categories. As a comparison, the deviances are also shown for Preston's ERR-LNT model.

	0-20 yr	20-40 yr	40-60 yr	60-80 yr	80 yr -	sum	Preston's ERR-LNT
							model
$D \le 0.005 \text{ Gy}$			149.09			149.09	149.90
$0.005 < D \le 0.1 \text{ Gy}$	0	13.73	131.23	273.93	168.23	587.12	597.72
$0.1 < D \le 0.5 \text{ Gy}$		623.38			623.38	626.25	
$0.5 < D \le 1 \text{ Gy}$	0	0.54	45.98	96.95	58.0	201.48	210.72
D > 1 Gy	225.35			225.35	226.66		

Table S5 Final deviances for cardiovascular diseases in females analyzed with EAR-LNT model: Final deviances obtained by forward calculations using the EAR-LNT model in combination with the mortality data for cardiovascular diseases in females. For the calculations the best estimates from Table S2 were applied. Data were grouped into five dose categories and five age categories. As a comparison, the deviances are also shown for Preston's ERR-LNT model.

	0-20 yr	20-40 yr	40-60 yr	60-80 yr	80 yr -	sum	Preston's ERR-LNT
							model
$D \le 0.005 \text{ Gy}$		127.09					128.96
$0.005 < D \le 0.1 \text{ Gy}$	614.56					614.56	612.06
$0.1 < D \le 0.5 \text{ Gy}$	0	7.87	65.92	307.03	179.71	560.52	568.84
$0.5 < D \le 1 \text{ Gy}$	0	0.85	33.02	103.08	54.62	191.56	195.22
D > 1 Gy	284.79					284.79	288.76