Identifying and Interpreting Subgroups in Health Care Utilization Data with Count Mixture Regression Models -Online Supplement

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Appendix

			high	overla	р		mediu	m over	·lap		low	overla	р
Component	N	β_0	β_1	β_2	$\overline{\psi}$	β_0	β_1	β_2	$\overline{\psi}$	β_0	β_1	β_2	$\overline{\psi}$
1	3000	0.0	0.5	-0.5	1.00	0.0	0.5	-0.5	1.00	0.0	0.5	-0.5	1.00
2	5000	1.0	0.0	0.0	13.25	1.8	0.0	0.0	25.75	3.2	0.0	0.0	50.75
3	3000	1.7	-0.5	0.5	25.50	2.4	-0.5	0.5	50.50	3.9	-0.5	0.5	100.50
4	4000	2.0	0.0	0.0	37.75	2.7	0.0	0.0	75.25	4.3	0.0	0.0	150.25
5	2000	2.3	0.5	-0.5	50.00	3.0	0.5	-0.5	100.00	4.6	0.5	-0.5	200.00

Table 1: Data-generating parameters for the simulation study. N indicates the number of simulated observations from each component.

			Comp.	1				Comp.	2	
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2
est.	0.0	0.4	-0.5	1.2	0.59	3.0	0.5	-0.5	83.7	0.41
truth	0.0	0.5	-0.5	1.0	0.60	3.0	0.5	-0.5	100	0.40

Table 2: Comparison of true and estimated parameters for the case with 2 components and medium overlap, where the number of mixture components was accurately estimated by MD-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

		(Comp.	1				Comp	. 2				Comp	o. 3				Comp.	4	
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2	β_0	β_1	β_2	ψ	c_3	β_0	β_1	β_2	ψ	c_4
est.	-0.1	0.6	-1.0	3.2	0.18	1.0	0.0	0.0	8.9	0.45	2.0	0.0	0.0	11.1	0.21	2.3	0.5	-0.5	61.9	0.16
truth	0.0	0.5	-0.5	1.0	0.21	1.0	0.0	0.0	13.25	0.36	2.0	0.0	0.0	37.75	0.29	2.3	0.5	-0.5	50.0	0.14

Table 3: Comparison of true and estimated parameters for the case with 4 components and high overlap, where the number of mixture components was accurately estimated by MD-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

								Comp	. 2			(Comp.	3				Comp	. 4				Comp.	5	
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2	β_0	β_1	β_2	ψ	<i>c</i> ₃	β_0	β_1	β_2	ψ	c4	β_0	β_1	β_2	ψ	c_5
est.	0.0	0.6	-1.0	1.5	0.12	1.3	0.0	0.1	6.8	0.34	1.6	-0.6	0.5	18.1	0.26	2.1	-0.2	0.1	39.3	0.17	2.3	0.5	-0.5	72.5	0.12
truth	0.0	0.5	-0.5	1.0	0.18	1.0	0.0	0.0	13.25	0.29	1.7	-0.5	0.5	25.5	0.18	2.0	0.0	0.0	37.75	0.24	2.3	0.5	-0.5	50.0	0.12

Table 4: Comparison of true and estimated parameters for the case with 5 components and high overlap, where the number of mixture components was accurately estimated by MD-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

		0.4 -0.7 1.5 0.10 1.8 0.0 0.0 6.9 0.34							(Comp.	3				Comp	. 4				Comp.	5				
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2	β_0	β_1	β_2	ψ	c_3	β_0	β_1	β_2	ψ	c_4	β_0	β_1	β_2	ψ	c_5
est.	-0.1	0.4	-0.7	1.5	0.10	1.8	0.0	0.0	6.9	0.34	2.4	-0.5	0.5	22.5	0.27	2.8	0.0	0.0	42.3	0.17	3.0	0.5	-0.5	66.2	0.13
truth	0.0	0.5	-0.5	1.0	0.18	1.0	0.0	0.0	13.25	0.29	1.7	-0.5	0.5	25.5	0.18	2.0	0.0	0.0	37.75	0.24	2.3	0.5	-0.5	50.0	0.12

Table 5: Comparison of true and estimated parameters for the case with 5 components and medium overlap, where the number of mixture components was accurately estimated by MD-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

					. 2				Comp	. 3				Comp	o. 4				Comp	. 5					
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2	β_0	β_1	β_2	ψ	c_3	β_0	β_1	β_2	ψ	C4	β_0	β_1	β_2	ψ	c_5
est.	0.1	0.5	-0.6	1.5	0.21	3.2	0.0	0.0	3.6	0.20	3.9	-0.5	0.5	43.3	0.23	4.3	-0.1	0.0	81.0	0.22	4.3	0.1	-0.3	208.3	0.14
truth	0.0	0.5	-0.5	1.0	0.18	3.2	0.0	0.0	50.75	0.29	3.9	-0.5	0.5	100.5	0.18	4.3	0.0	0.0	150.25	0.24	4.6	0.5	-0.5	200.0	0.12

Table 6: Comparison of true and estimated parameters for the case with 5 components and low overlap, where the number of mixture components was accurately estimated by MD-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

			Comp.	1				Comp.	2	
	β_0	eta_1	eta_2	ψ	c_1	β_0	eta_1	β_2	ψ	c_2
est.	0.0	0.4	0.5	1.0	0.60	2.3	-0.7	-0.5	60.8	0.40
truth	0.0		-0.5			3.0		-0.5		0.40

Table 7: Comparison of true and estimated parameters for the case with 2 components and high overlap, where the number of mixture components was accurately estimated by LOG-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

			Comp.	1			(Comp.	2	
	β_0	eta_1	eta_2	ψ	c_1	β_0	eta_1	eta_2	ψ	c_2
est.	0.0	0.5	0.5	1.0	0.60	4.6	-0.6	-0.5	221	0.40
truth	0.0	0.5	-0.5	1.0	0.60	4.6	0.5	-0.5	100	0.40

Table 8: Comparison of true and estimated parameters for the case with 2 components and low overlap, where the number of mixture components was accurately estimated by LOG-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

			Comp.	1				Comp	. 2				Comp.	3	
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2	β_0	β_1	β_2	ψ	<i>c</i> ₃
est.	0.3	0.2	-0.4	22.4	0.37	0.9	0.3	-0.3	5.7	0.46	2.3	0.5	-0.5	159	0.17
truth	0.0	0.5	-0.5	1.0	0.3	1.0	0.0	0.0	13.25	0.5	2.3	0.5	-0.5	50	0.2

Table 9: Comparison of true and estimated parameters for the case with 3 components and high overlap, where the number of mixture components was accurately estimated by LOG-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

3 Comp.			Comp.	1				Comp	. 2			(Comp.	3	
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2	β_0	β_1	β_2	ψ	<i>c</i> ₃
est.	0.7	0.2	-0.3	20.1	0.35	1.8	0.1	-0.2	35	0.47	3.0	0.5	-0.5	203	0.2
truth	0.0	0.5	-0.5	1.0	0.3	1.8	0.0	0.0	25.75	0.5	3.0	0.5	-0.5	100	0.2

Table 10: Comparison of true and estimated parameters for the case with 3 components and medium overlap, where the number of mixture components was accurately estimated by LOG-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

			Comp.	1				Comp	. 2				Comp	. 3				Comp	o. 4				Comp	. 5	
	β_0	β_1	β_2	ψ	c_1	β_0	β_1	β_2	ψ	c_2	β_0	β_1	β_2	ψ	c_3	β_0	β_1	β_2	ψ	c_4	β_0	β_1	β_2	ψ	<i>c</i> ₅
est.	0.1	0.5	-0.6	3.4	0.21	3.2	0.0	0.0	28.9	0.23	3.7	-0.5	0.6	61.3	0.22	4.3	0.0	0.0	102.0	0.22	4.7	0.5	-0.5	232.4	0.12
truth	0.0	0.5	-0.5	1.0	0.18	3.2	0.0	0.0	50.75	0.29	3.9	-0.5	0.5	100.5	0.18	4.3	0.0	0.0	150.25	0.24	4.6	0.5	-0.5	200.0	0.12

Table 11: Comparison of true and estimated parameters for the case with 5 components and low overlap, where the number of mixture components was accurately estimated by LOG-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. All estimates are based on posterior medians. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

		Coı	np. 1			Co	mp. 2			Cor	np. 3			Cor	mp. 4	
	β_0	β_1	β_2	c_1	β_0	β_1	β_2	c_2	β_0	β_1	β_2	c_3	β_0	β_1	β_2	c_4
est.	2.3	0.2	-0.2	0.26	2.3	0.2	-0.2	0.38	2.3	0.1	-0.2	0.28	2.3	0.2	-0.2	0.08
truth	0.0	0.5	-0.5	0.21	1.0	0.0	0.0	0.36	2.0	0.0	0.0	0.29	2.3	0.5	-0.5	0.14

Table 12: Comparison of true and estimated parameters for the case with 4 components and medium overlap, where the number of mixture components was accurately estimated by MLE-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

	Comp. 1				Comp. 2				Comp. 3				Comp. 4			
	β_0	β_1	β_2	c_1	β_0	eta_1	β_2	c_2	β_0	eta_1	β_2	c_3	β_0	β_1	β_2	c_4
est.	-0.3	0.5	-0.6	0.20	3.9	0.2	-0.2	0.77	4.4	0.2	-0.2	0.02	4.5	0.5	-0.5	0.01
truth	0.0	0.5	-0.5	0.21	1.0	0.0	0.0	0.36	2.0	0.0	0.0	0.29	2.3	0.5	-0.5	0.14

Table 13: Comparison of true and estimated parameters for the case with 4 components and low overlap, where the number of mixture components was accurately estimated by MLE-NB. β 's indicate intercept and regression coefficients and c's are the mixture weights. Because the estimated mixture components are not always in the same order, estimated components were hand-matched to their corresponding best-fitting component.

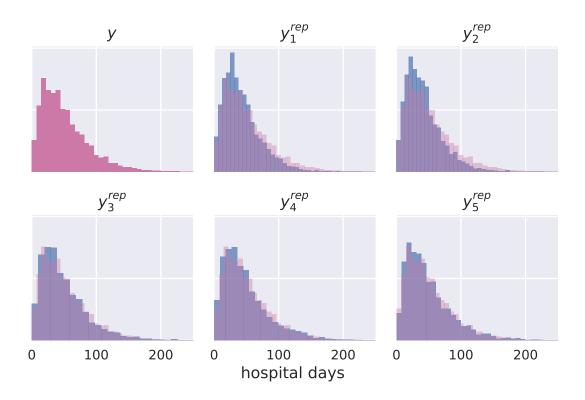


Figure 1: Density histograms for replicated outcome y^{rep} from simulating data from the posterior predictive distribution using the observed predictors. True outcome y from the AOK data set for comparison.

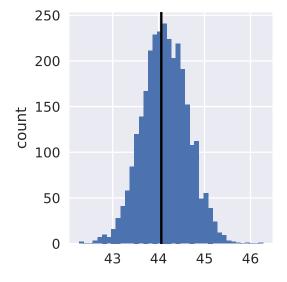


Figure 2: Histogram of means based on 1000 replicated data sets from the posterior predictive distribution. The black line marks the observed mean of hospital days from the AOK data set.

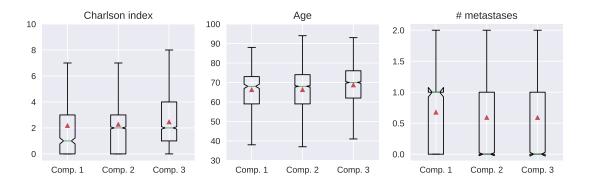


Figure 3: Boxplots for Charlson comorbidity index, age, and the number of metastases after using hard component assignments based on the MD-ZINB for the AOK data set. The red triangle marks the mean.